



Atomic radiations in nuclear decay

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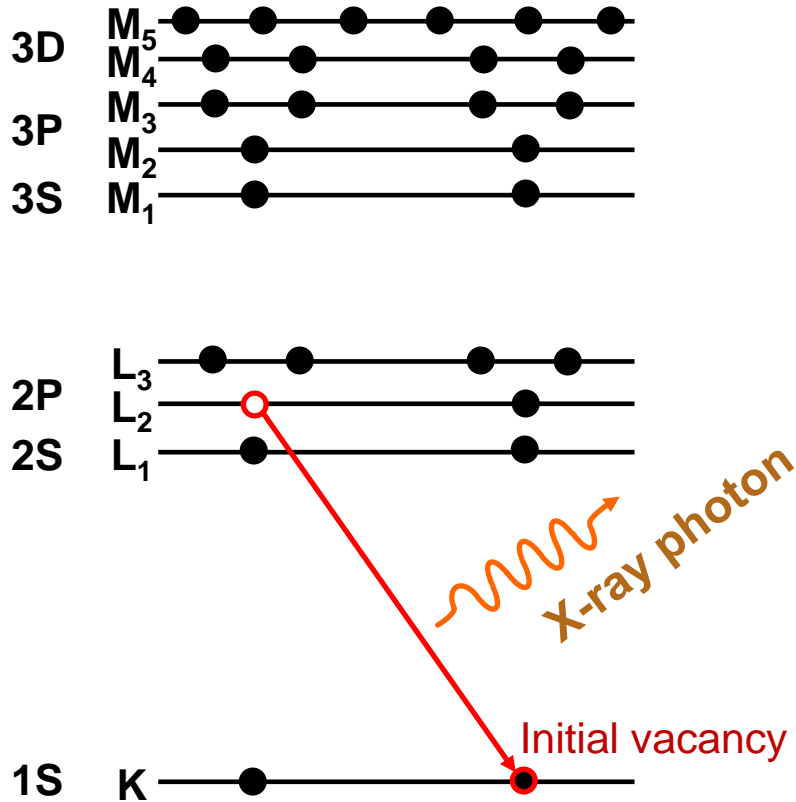
Talk is largely based on

Kálmán Robertson (ANU) , Honours project, October 2010 (literature review, new model of Non-radiative transition rates)

Boon Quan Lee (ANU), special research project (BrIccEmission)

- **Radiative and Non-radiative atomic transitions in nuclear decay**
- **Nuclear and atomic data**
- **Existing programs to evaluate atomic radiations**
- **New model to evaluate Non-radiative transition energies and rates**
- **Future directions**

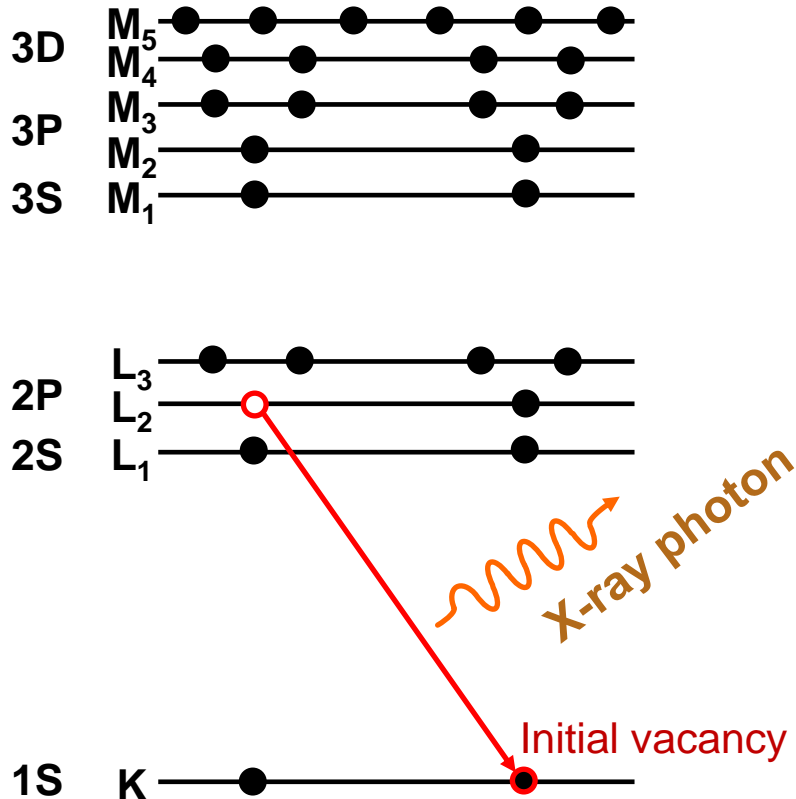
X-ray emission



$$E_{X_{K\alpha 2}} = E_K - E_{L2}$$

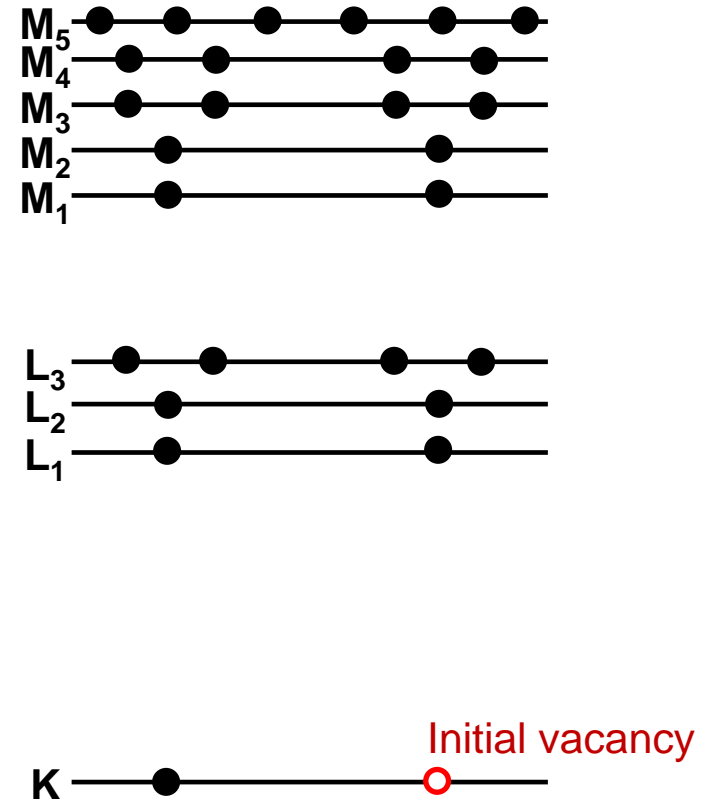
K α 2 X-ray
1 secondary vacancy

X-ray emission



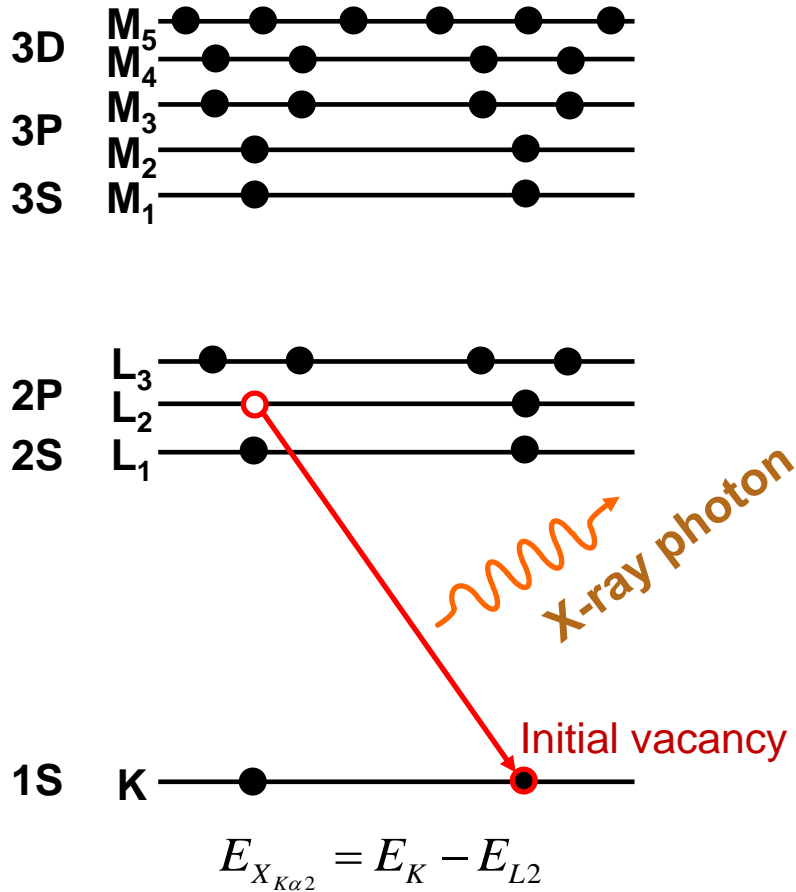
$$E_{X_{K\alpha 2}} = E_K - E_{L2}$$

K α 2 X-ray
1 secondary vacancy



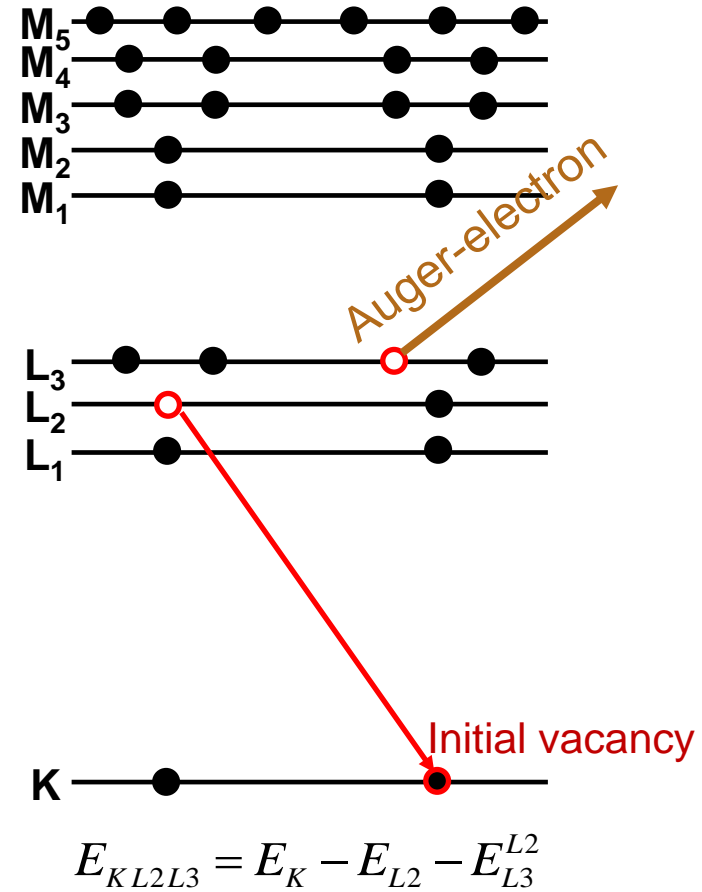
Atomic radiations - Basic concept

X-ray emission



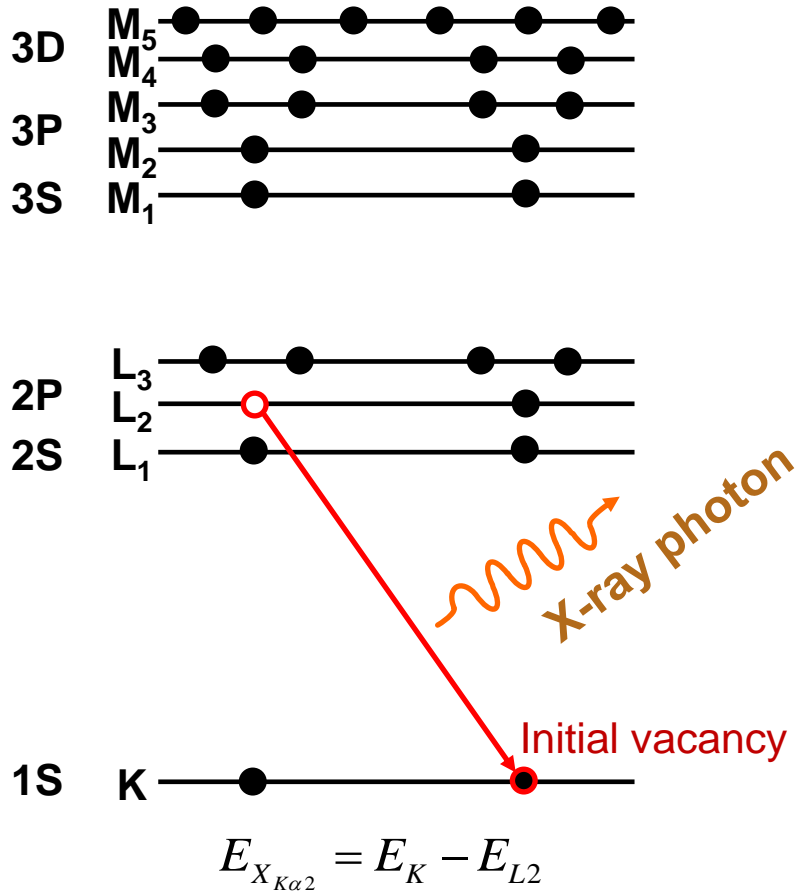
K α 2 X-ray
1 secondary vacancy

Auger-electron



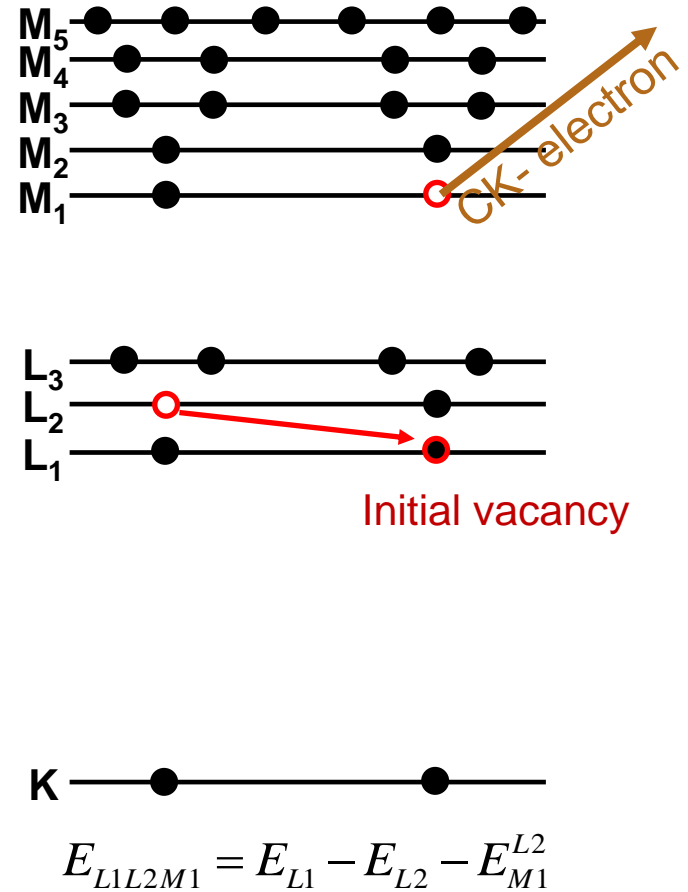
K L2 L3 Auger-electron
2 new secondary vacancies

X-ray emission



K α 2 X-ray
1 secondary vacancy

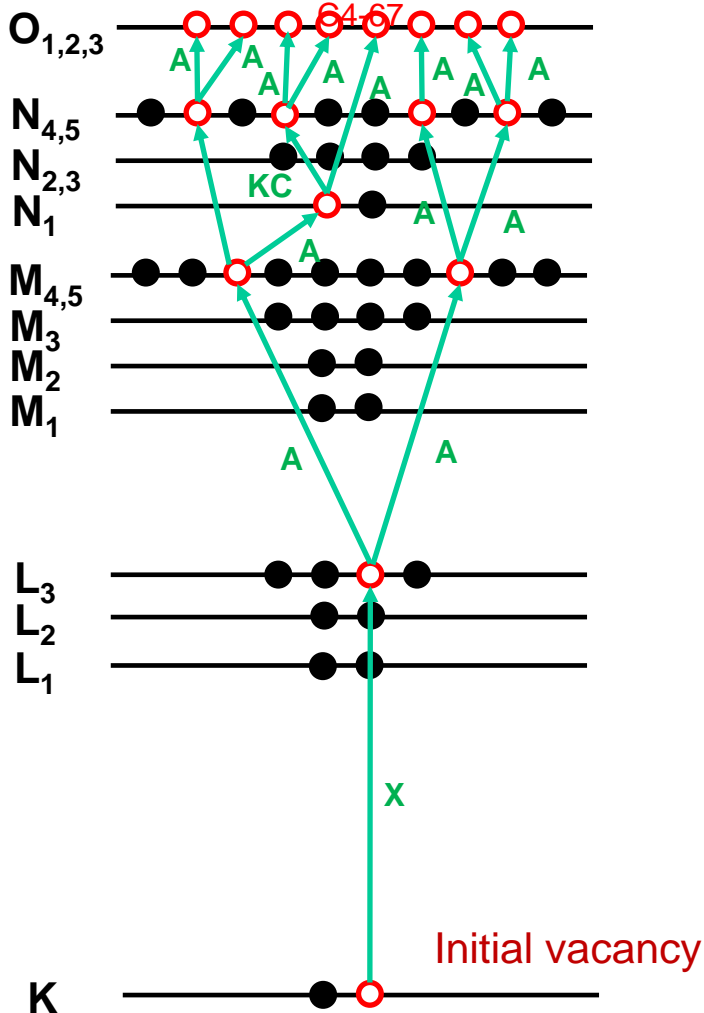
Coster-Kronig electron



L1 L2 M1 Coster-Kronig transition
2 new secondary vacancies

A vacancy cascade in Xe

From M.O. Krause, J. Phys. Colloques, 32 (1971)



- Full relaxation of an initial inner shell vacancy creates vacancy cascade involving **X**-ray (Radiative) and **A**uger as well as **C**oster-**K**ronig (Non-Radiative) transitions
- Many possible cascades for a single initial vacancy!
- Typical relaxation time $\sim 10^{-15}$ seconds!
- Many vacancy cascades following a single ionisation event!

For a single initial vacancy on the K-shell following nuclear decay

Number of primary vacancies

Internal conversion

$$n_K = P_\gamma \times \frac{\alpha_K}{1 + \alpha_T}$$

Electron capture

$$n_K = P_\varepsilon \times P_K$$

X-ray emission

Auger-electron

Energy

$$E_{X_{KY}} = E_K - E_Y$$

$$E_{KXY} = E_K - E_X - E_Y^X$$

in an ion

Intensity

$$I_{X_{KY}} = n_K \times \omega_K$$

$$I_{KXY} = n_K \times a_K$$

$$\omega_K + a_K \equiv 1$$

for L1 shell

$$I_{X_{L1Y}} = n_{L1} \times \omega_{L1}$$

$$I_{L1XY} = n_K \times (a_{L1} + f_{L1L2} + f_{L1L3})$$

$$\omega_{L1} + a_{L1} + f_{L1L2} + f_{L1L3} \equiv 1$$

Nuclear data

ENSDF continuously updated

2008Ki07, 2002Ba85 (Brlcc): *Conversion coefficients*

1998Sc28, Schönfeld : *Electron Capture Probabilities*

EC program Schönfeld, Chu & Brown

Atomic Data (incomplete)

1972Bb16, Bambynek et al.,: *X-Ray Fluorescence Yields, Auger, and Coster-Kronig Transition Probabilities*

1984 update in an Conf. Proc.

1977La19, Larkins: *Semi-empirical Auger energies (for single initial vacancies only!)*

1979Kr13, Krause, *Radiative and Non-Radiative Yields for K and L Shells*

Atomic Data (cont)

Evaluated Atomic Data Library (EADL),

[1] D.E. Cullen, et al., "Tables and Graphs of Atomic Subshells and Relaxation Data Derived from the LLNL Evaluated Atomic Data Library (EADL), $Z = 1 - 100$," Lawrence Livermore National Laboratory, UCRL-50400, Vol. 30, October 1991.

[2] D.E. Cullen "Program RELAX: A Code Designed to Calculate X-Ray and Electron Emission Spectra as Singly Charged Atoms Relax Back to Neutrality," Lawrence Livermore National Laboratory, UCRL-ID-110438, March 1992.

X-ray, Auger and Coster-Kronig energies & transition rates for single vacancies

Neutral atom binding energies, primary source of atomic data need to be confirmed!

Atomic Data (cont.)

- **1994Hu23, Hubbell et al.:** *Review, Bibliography, and Tabulation of K, L, and higher atomic shell X-Ray Fluorescence Yields*
many errors found, see **J. Phys. Chem. Ref. Data, 33 (2004) 621!**
- **1995ScZX, 1996Sc06, Schönfeld and Janssen:** *absolute K and L X-ray rates*
- **2007Pu05, Puri:** *rel. L and M X-ray intensities*
- **2009 Campbell (ADNDT 95 p115; not in NSR)**
L1 Fluorescence and Coster-Kronig Probability
- **2009 Campbell for Group 4:** *review of atomic data X-ray transition and Coster-Kronig transition probabilities*
 - *primary source of data often not clearly stated*
 - *1996Sc06 Scofield no data for $Z < 30$*
 - *Last extensive theoretical DF work by Scofield (1974)*
 - *L-shell: extensive review is long overdue*
 - *M-shell almost no data*
 - *Should theory being used to fill the gaps in systematics?*

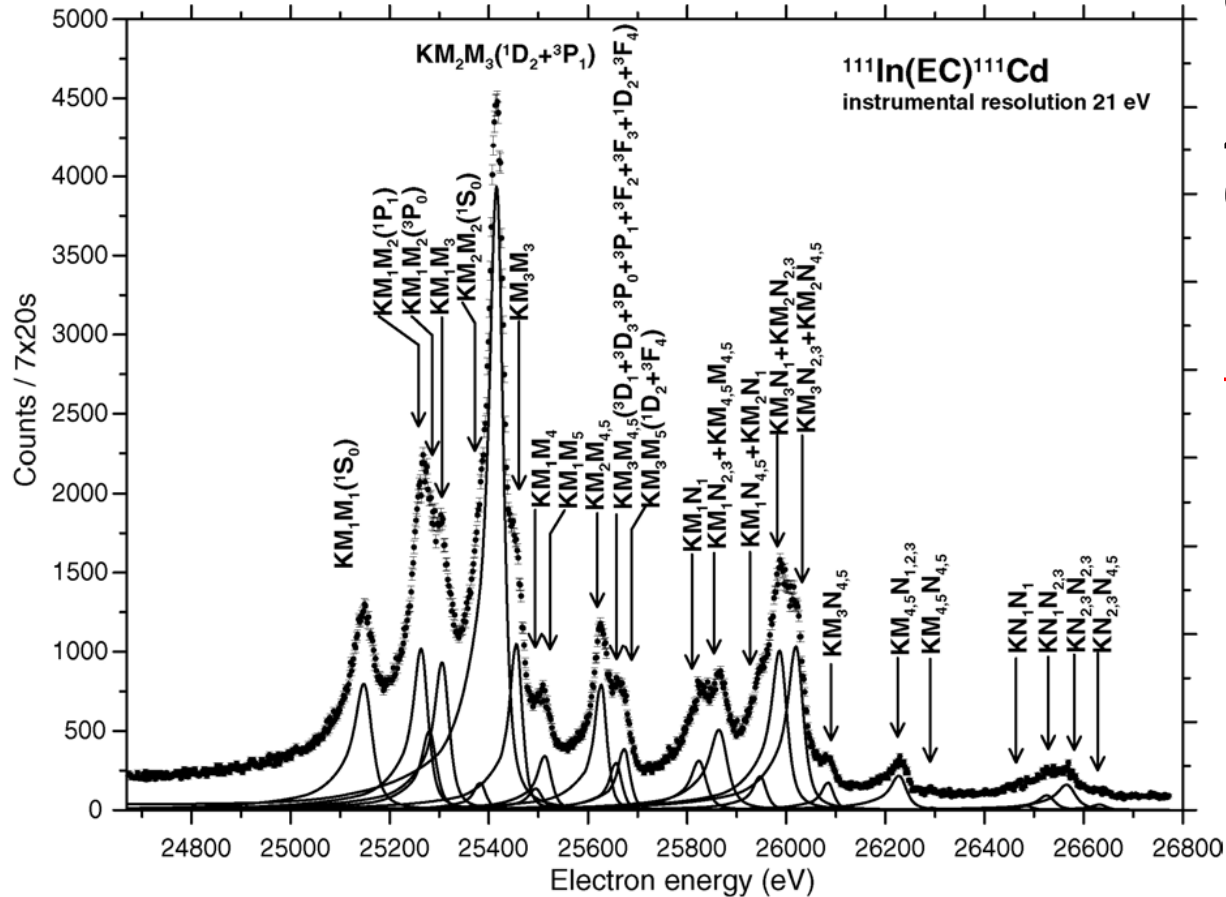
Existing programs/data bases

	Nucl Data	Atomic Data	Atomic Radiations	Comment
EDISTR Dillman (1985)	ENSDF	unknown	unknown	NEA PSR-0191 EDISTR.
RADLST Burrows (1988)	ENSDF, Hslcc	1972Bb16 Bambynek	K,L X-rays and Auger	Used for MIRD
RELAX Cullen (1992)	ENDL	EADL	K,L,M,N X-rays and Auger	Neutral atom BE
IMRDEC Stepanek (1997)	ENSDF, own ICC	EPDL, EEDL	K,L,M,N X- rays and Auger	Bug: decay parent BE used; only Monte-Carlo vacancy propagation program
EMISSIN Schönfeld & Janssen (2000)	Manual DDEP	1995ScZX 1996Sc06 Schönfeld	K,L X-rays and Auger	Inaccurate below Z=25; Extended for L subs-shell 2006Be35 Marie-Martine Be

Common problems / limitations

- Neutral atom binding energies are used for atoms with vacancies; i.e. for ions
- Single initial vacancy is considered. Secondary vacancies are ignored
- Atomic radiations only from K and L shell
- Limited information on sub-shell rates
- Auger spectrum below ~ 1 keV is often omitted

A. Inoyatov et al. / *Journal of Electron Spectroscopy and Related Phenomena* 151 (2006) 193–198



Only a handful data on KMM Auger-electrons:
Z=25, 26, 36, 46, 54, 62, 69, 78, 84

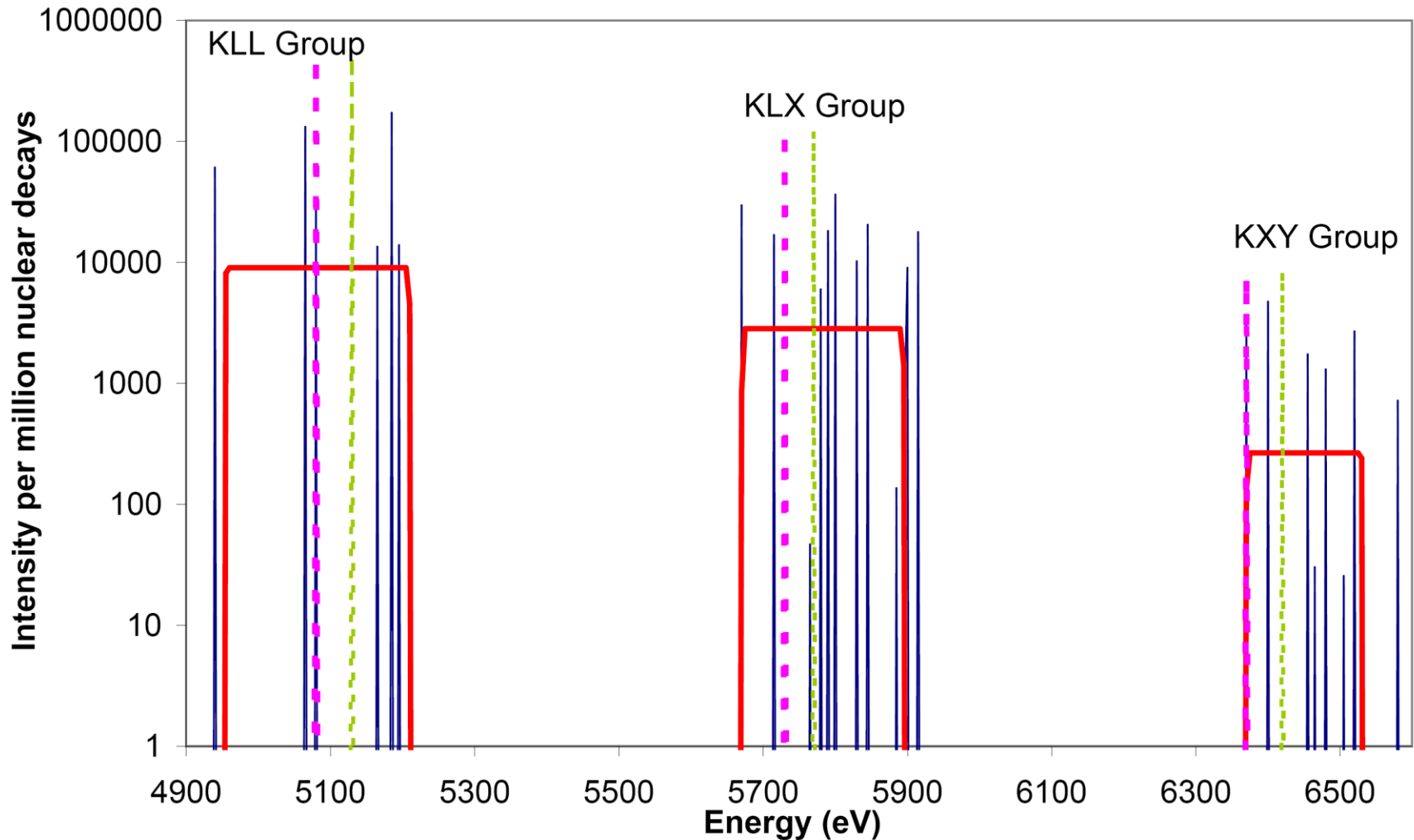
Need to extend theoretical models beyond L-shell

KNN Auger spectrum of ^{111}Cd from the EC-decay of ^{111}In measured with 21 eV instrumental resolution and 2 eV resolution with an exposition of 20 s per point in each sweep. Results of the spectrum decomposition into components are

New model to evaluate Non-Radiative transitions (Kalman's model)

- Primary vacancies from Brcc (for CE) and EC (for electron capture)
- Binding energies calculated using RAINE for electron configurations of a neutral atom or an ion with single or multiple vacancies
- Auger and CK transition rates calculated using non-relativistic perturbation theory with screened hydrogenic wave functions (Simple general formalism for all shells and transitions)
- Propagate vacancies until they reach valence shells (or the shells immediately below)
- Partially Defrosted Orbitals: calculations for all electronic configurations (complete treatment) but using single-vacancy transition rates

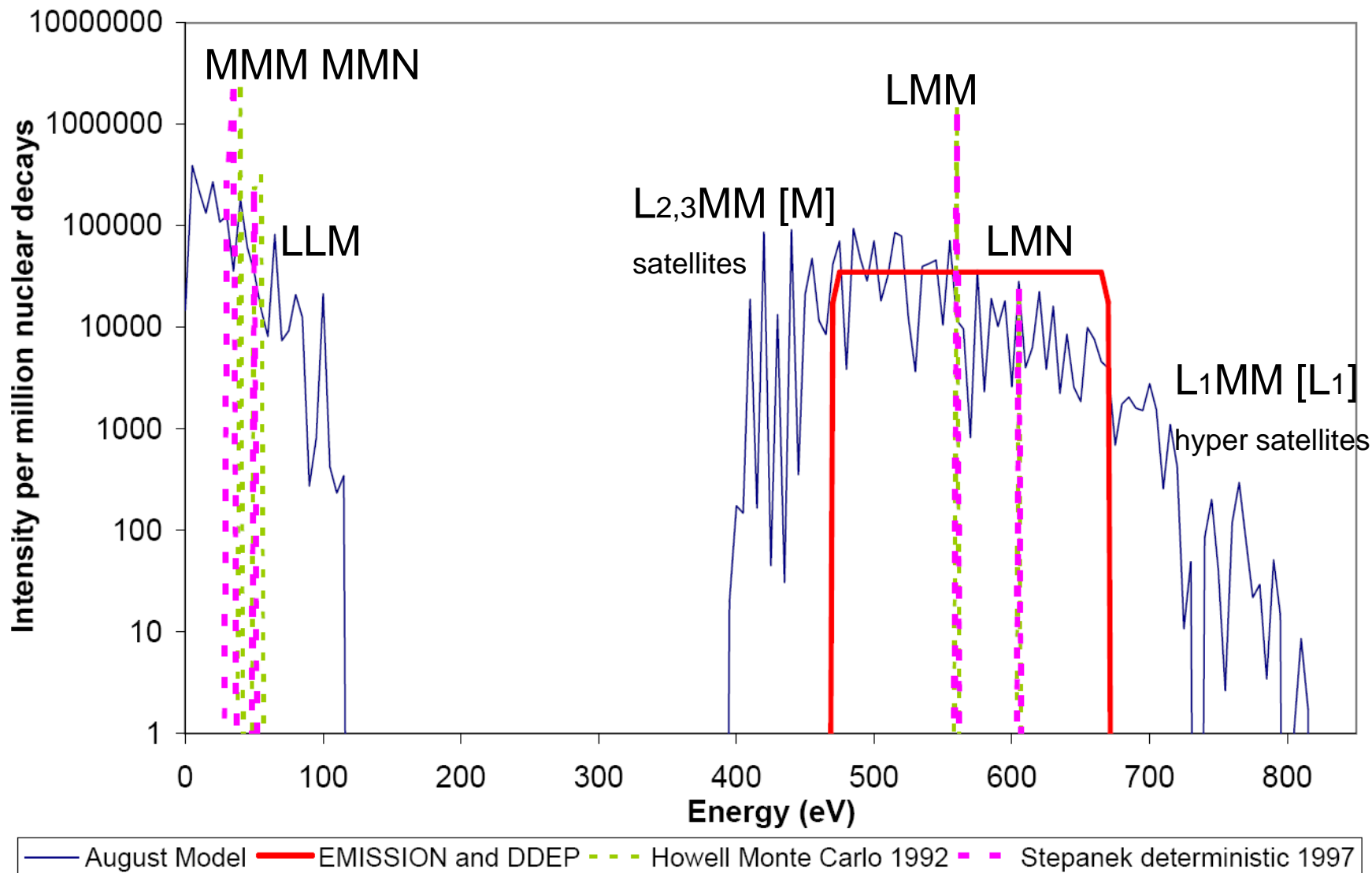
$^{55}\text{Fe} + e^- \rightarrow ^{55}\text{Mn} + \nu$ K-Auger electrons (5 eV bins)





3.7×10^6 Auger electrons and 2.8×10^5 X-rays per 10^6 nuclear decays

L- and *M*- Auger electrons (5 eV bins)



- Uses ENSDF file for input nuclear structure data
- Uses atomic data from Schönfeld and Janssen (1995ScZX, 1996Sc06)
- Calculates X-ray and Auger-electron spectrum for K and L shell
- Future plans:
 - Calculate theoretical binding energies using the RAINE code
 - Incorporate up-to date atomic data on X-ray emission
 - Incorporate Kalman`s model to calculate detailed energy spectra of Auger and Coster-Kronig transitions

Results:

Vacancy Creation:

N(K)	:	0.8853(17)
N(L)	:	1.407(5)
N(L1)	:	0.314(5)
N(L2)	:	0.515(6)
N(L3)	:	0.576(7)

Auger Yield:

a(K)	:	0.679(5)
a(L1)	:	0.044(16)
a(L2)	:	0.99660(20)
a(L3)	:	0.99610(20)

X-Ray Emission Probabilities:

	Intensity	Energy(kev)	
p(XK)	0.284(5)		
p(XL)=N(L)*<OmegaL>	0.0066(10)		
p(XL1)	0.000104(7)		
p(XL2)	0.00204(13)		
p(XL3)	0.00309(17)		
p(XL)=p(XL1)+p(XL2)+p(XL3)	0.00523(21)		
p(KAlpha)	0.250(4)		
p(KBeta)	0.0340(7)		
p(KAlpha1)(K-L3)	0.166(3)		5.899(0)
p(KAlpha2)(K-L2)	0.0845(14)		5.888(0)
p(K'Beta1)(K-M2,3,4,5)	0.0340(7)	6.486(0)	6.536(0)
p(K'Beta2)(K-N2,3,4,5)	0.000(0)	6.539(0)	6.539(0)

Partial L-Shell X-Ray Emission Probability:

pX(L1-M2)	p(XLBeta4)	3.60E-5(23)	0.7159(0)
pX(L1-M3)	p(XLBeta3)	6.8E-5(5)	0.7226(0)
pX(L2-M1)	p(XLEta)	0.00204(13)	0.5675(0)
pX(L3-M1)	p(XL1)	0.00309(17)	0.5564(0)

Auger Electron Emission Probability: Intensity

K-Shell

p(eaK)	: 0.601(5)
p(KLL)	: 0.466(4)
p(KLX)	: 0.1267(18)
p(KXY)	: 0.00862(20)

L-Shell

p(eaL)=N(L)*(1-<Omega>)	: 1.400(5)
p(eaL1)	: 0.014(5)
p(eaL2)	: 0.597(6)
p(eaL3)	: 0.789(9)
p(eaL)=p(eaL1)+p(eaL2)+p(eaL3)	: 1.400(12)

- Existing atomic data on X-ray, Auger and Coster-Kronig transitions is incomplete
- Existing programs only cover radiations from single vacancies on the K and L-shell. Sub-shell transition rates are often not known. Neutral binding energies are used.
- New program being developed to treat all atomic shells and multiple vacancies to evaluate detailed energy spectra of atomic radiations using ENSDF file as input for nuclear structure data